



Design of anti-icing surfaces: smooth, textured or slippery?

Citation

Kreder, Michael J., Jack Alvarenga, Philseok Kim, and Joanna Aizenberg. 2016. "Design of Anti-Icing Surfaces: Smooth, Textured or Slippery?" *Nature Reviews Materials* 1 (1) (January). doi:10.1038/natrevmats.2015.3.

Published Version

doi:10.1038/natrevmats.2015.3

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Smooth, textured or slippery? Modern approaches to anti-icing materials

Michael J. Kreder,¹ Jack Alvarenga,² Philseok Kim,² Joanna Aizenberg*¹⁻⁴

¹John A. Paulson School of Engineering and Applied Sciences; ²Wyss Institute for Biologically Inspired Engineering; ³Department of Chemistry and Chemical Biology; ⁴Kavli Institute for Bionano Science and Technology, Harvard University, Cambridge, MA 02138.

Passive anti-icing surfaces, or icephobic surfaces, are an area of great interest because of their significant economic, energy and safety implications in the prevention and easy removal of ice in many facets of society. The complex nature of icephobicity, which requires performance in a broad range of icing scenarios, creates many challenges when designing ice-repellent surfaces. Although superhydrophobic surfaces incorporating micro- or nanoscale roughness have been shown to prevent ice accumulation under certain conditions, the same roughness can be detrimental in other environments. Surfaces that present a smooth liquid interface can eliminate some of the drawbacks of textured superhydrophobic surfaces, but additional study is needed to fully realise their potential. As more attention begins to shift towards alternative anti-icing strategies, it is important to consider and understand the nature of ice repellency in all environments to identify the limitations of current solutions and design new materials with robust icephobicity.

Introduction

History of Water Repellent Surfaces. The ability to design materials that can withstand environmental challenges has been important for survival throughout human history. Critical issues, such as crop spoilage due to moisture contamination and hypothermia caused by the loss of body heat associated with wet clothing, provided early motivation for protective barriers that could effectively repel water in various forms, from condensed moisture to rain, snow and ice. Although some species have evolved features that allow them to resist the detrimental effects of water, such as the structure and hydrophobic properties of duck feathers, which can resist water penetration¹, humans have needed to develop broader technologies for repelling moisture in a variety of situations. Typically, this has involved the selection of well-suited materials from nature, such as animal furs or natural fibres, which could then be further improved by incorporating natural oils and waxes to withstand harsh environments^{2,3}. Such strategies provided the basis for water repellency until modern understanding of liquid–solid interactions allowed the design of more advanced materials.

Pioneering work explained the nature of solid–liquid interactions, including wetting and non-wetting scenarios. In 1805, Thomas Young described the equilibrium behaviour of a droplet on an ideal

surface⁴. Deviations in the contact angle of a droplet on a solid surface, which are critical to liquid adhesion and mobility, were first described as ‘hysteresis’ by the metallurgy community in the early 1900s⁵, but the phenomenon was considered at least as far back as Gibbs’ work on the thermodynamic properties of surfaces that included a discussion of ‘the frictional resistance to a displacement of the [contact] line’⁶, and so-called ‘contact angle hysteresis’ continues to be investigated today^{7–10}. Later developments led to further understanding of nonideal surfaces through the Wenzel¹¹ and Cassie–Baxter^{1,12} equations. For those readers who are unfamiliar with this foundational work, these theories are briefly described in Text Box 1, and in detail by de Gennes *et al.*¹³. Together, these theories established the surface characteristics that are required to yield highly effective water-repellent materials. A timeline of several major advances in repellency following Young’s work is presented in Fig. 1.

((Textbox 1))

((Figure 1))

One of the key materials advances in the development of water repellent surfaces was the discovery of natural rubbers and the subsequent development of synthetic polymers in the 1900s¹⁴. This led to the development of critical low-surface-energy polymers such as PDMS (polydimethylsiloxane, a common silicone rubber) and PTFE (commonly known as Teflon™ or polytetrafluoroethylene). Furthermore, by introducing porosity, PTFE could be made breathable and with improved ability to repel water – a discovery that revolutionized the high-performance textile industry. These polymers can often be applied as coatings on various materials to modify surface wettability. The development of an alternative method for introducing low-surface-energy chemistry, which involves the creation of molecular-scale, self-assembled monolayers (SAMs), allowed for the precise control of the surface chemistry and repellency of certain materials¹⁵.

In the late 1990s, advances in visualisation and fabrication techniques sparked rapid developments in the area of water repellency. Specifically, the ability to visualise and replicate the structure of the lotus leaf enabled the production of synthetic superhydrophobic surfaces (SHS) by combining micro- and nanoscale texture and hydrophobic surface chemistry, resulting in very high water contact angles ($\geq 150^\circ$) and low contact angle hysteresis (CAH; $\leq 5^\circ$)^{16,17}. These discoveries led to a phase of extensive development, which saw SHS produced from a wide array of materials and processes, with a concomitant improvement in performance and stability, and increased fundamental understanding^{18–22}. The incorporation of re-entrant^{23,24} and eventually double re-entrant²⁵ curvatures led to more robust repellency, resisting even low-surface-energy liquids that would completely wet typical nanostructured SHS.

Although this complex surface structuring introduced enhanced repellency, the voids between surface features can serve as vulnerabilities under harsh environmental conditions. This problem was addressed by creating a new class of functional materials – slippery liquid-infused porous surfaces (SLIPS)

– in which a textured solid is infiltrated with a physically and chemically confined immiscible lubricant to create a smooth liquid overlayer. These resulting surfaces are stable under high pressure, exhibit essentially no contact angle pinning and are omniphobic^{26–29}. Inspired by this approach, a variety of fabrication techniques for producing functional slippery surfaces have been reported, expanding the types of materials and potential applications this technology can impact^{30–37}.

Surfaces with low water wettability have been developed to possess many beneficial properties, such as fluid flow drag reduction, increased heat transfer and improved self-cleaning ability^{38–42}. In the challenging area of ice repellency, it has been shown that surfaces with low water wettability offer great promise as passive anti-icing – or ‘icephobic’ – surfaces^{40,41,43}; however, water repellency alone is not sufficient. Icephobic surfaces also require the ability to significantly suppress ice nucleation, impede frost formation and reduce ice adhesion forces. This challenging problem will form the focus of this Review.

The Nature of Icing Problems. Despite numerous advances in the development of repellent coatings, problems of ice accretion remain significant^{40,44,45}. Various critical structures, such as power lines and buildings, can be damaged by the excessive weight of accumulated ice and the stress caused by freeze–thaw cycles, and severe personal injury can result from falling ice. Such hazards are exacerbated by extreme conditions, isolation, and the preponderance of water in marine environments on ships and off-shore oil rigs⁴⁵. Transmission line and tower failures have caused notorious power outages, such as those caused by a 2008 ice storm in the Northeast U.S., which left over one million people without power with an estimated cost exceeding one billion dollars. The efficiency and output of renewable energy sources, including wind and solar, can also be severely impacted by ice formation^{43,46–48}. Ice accumulation on aircraft is responsible for numerous problems such as frequent delays, increased drag, additional cost for deicing, and contamination of ground water due to the salts and glycols used in the deicing fluids^{49,50}, in addition to numerous and recent fatal crashes. Frost formation in a humid environment on cold solid surfaces, such as those commonly encountered in thermal management systems, can substantially reduce the heat transfer efficiency, with additional energy consumed during necessary defrosting cycles^{40,41,51,52}.

The diversity of icing problems presents many challenges. Icing conditions can only be controlled in certain environments. For example, heat exchangers may be designed to operate within narrow temperature and humidity ranges. However, in natural environments, ice accretion occurs over a wide range of temperatures, humidity levels and wind conditions owing to the many different forms of precipitation, including freezing rain, snow, in-cloud or fog icing, and frost formation^{44,45}. While it is typical for laboratory experiments to focus on a single aspect of icing, for many important applications icephobic surfaces require the ability to withstand a wide range of possible conditions. Current industry strategies for combatting icing problems primarily involve active heating, chemical deicing fluids and mechanical removal^{44,49,50,53}. These

processes can be inefficient, environmentally unfavourable, expensive and time consuming. Thus, it would be advantageous if surfaces could passively prevent ice formation and ease ice removal. In this Review, we critically examine the different strategies for attaining icephobicity for the different scenarios in which ice may form at surfaces.

Ice Formation from Impinging Droplets

Ice often accumulates when droplets of liquid water come into contact with surfaces at temperatures below the freezing point. This situation is commonly encountered in the form of freezing rain, and impacts power lines, aircraft and many other types of infrastructure^{43,49}. SHS, owing to their extraordinary water repellency, are viewed as excellent candidates for icephobicity in this area^{40,54}; however, their performance is still largely limited by environmental constraints. Preventing ice formation in this scenario can be separated into two main approaches: (i) minimising the contact time to promote rapid shedding of droplets before ice can nucleate on the surface, and (ii) delaying heterogeneous nucleation by a combination of surface roughness, chemistry and topographical modifications.

Minimised Contact Time. It is well known that, under certain conditions, water droplets that impact a SHS will retract and bounce from the surface owing to their extremely low CAH^{55,56}. Taking advantage of this phenomenon, SHS can dynamically eliminate ice formation, even if the surface is maintained at temperatures well below freezing, as shown in Fig. 2a^{57–62}. Mishchenko *et al.*⁵⁹ investigated impacting droplets with temperatures ranging from +60 to –5 °C on tilted substrates (30°) with surface temperatures from 20 to –30 °C. Ice formation on SHS was strongly dependent on the surface temperature, irrespective of the level of droplet undercooling. At surface temperatures above –25 °C, droplets were able to fully retract before freezing could occur on the SHS, whereas ice nucleated on smooth hydrophilic and hydrophobic surfaces⁵⁹. Bahadur *et al.*⁶³ developed a detailed ice-formation model for a droplet impacting a structured superhydrophobic surface that incorporated the droplet contact time, heat transfer and heterogeneous nucleation theory. In their model, when a droplet strikes a supercooled surface, ice crystals nucleate on the tips of the posts, causing a decrease in the retraction force of the impacting droplet that eventually leads to incomplete retraction, pinning and complete freezing of the droplet; if the droplet contact time is less than the time required to induce pinning, no ice forms. Good agreement was found between this transient model and experimental results. More generally, this demonstrated that the integration of multiple dynamic processes is required to predict whether a surface resists ice or not⁶³.

((Figure 2))

Much of the work looking at droplet impact on SHS has focused on increasing the stability of the Cassie state during droplet impingement in a freezing environment. Droplet bouncing occurs when the

impacting liquid maintains enough energy to depart the surface following losses during spreading and retraction; however, if a droplet strikes the surface with sufficient kinetic energy, it may displace the air pockets of the SHS and become pinned in the Wenzel state^{64–70}. Not only do droplets in this state have low mobility due to high contact line pinning, but their increased contact area with the underlying solid also improves heat transfer, leading to more opportunities for heterogeneous ice nucleation, even compared with topographically smooth hydrophobic surfaces⁴².

This transition is resisted by the Laplace pressure, which is the pressure difference across a curved interface caused by surface tension. The Laplace pressure can be increased by incorporating nanoscale topography^{65–69}, hierarchy⁷¹ or using closed-cell structures^{59,64}, thereby resisting the transition into the Wenzel state, as shown in Fig. 2b. Improved icephobicity against impinging droplets has been demonstrated using denser features^{57,59,72} or closed-cell structures⁵⁹; however, increasing the solid fraction may actually lead to decreased superhydrophobic performance⁶⁸. Ice nucleation could further be reduced by decreasing the contact time of bouncing droplets, which is possible by incorporating macroscopic texture on a SHS⁷³ but there is a practical limit to contact time on macroscopically smooth surfaces⁷³.

Another key consideration is the ability of SHS to retain icephobicity in harsh environmental conditions. Lower temperatures increase the viscosity of supercooled droplets thus increasing contact time and reducing the chance of bouncing⁷⁴. In general, the bouncing droplet effect is observed at low humidity levels. At surface temperatures below the dew point, the CAH of water droplets begins to increase owing to uniform nucleation across the surface topography of the microstructured SHS, which promotes non-bouncing Wenzel droplets^{75–78}. In some cases, SHS fail even in environments without bulk supersaturation because water droplets increase the humidity of their local environment⁶⁰. Thus, in situations of high humidity or when supersaturation is likely to occur (typically when the surface is colder than the surrounding environment), the bouncing-droplet effect is an ineffective path towards icephobicity. For this reason, it is important to carefully consider environmental conditions related to real-world scenarios when testing these surfaces.

Nucleation Reduction. Although the probability of nucleation can be reduced dynamically by promoting bouncing and rapid shedding of impinging droplets, it is also beneficial, particularly under static conditions, to delay heterogeneous nucleation through modification of surface topography and chemistry, which facilitates potential removal of liquid water by other means. The ability of various surfaces to delay the freezing of a sessile droplet has been extensively studied to characterise the relationship between superhydrophobicity and heterogeneous ice nucleation, albeit with conflicting results. Many groups have found significantly delayed nucleation on microstructured SHS^{58,59,62,63}, whereas others have found that nucleation is influenced more strongly by nanoscale roughness^{57,75,79} or can further be influenced by

hierarchical texture⁸⁰. These discrepancies can be explained, at least in part, by the complexity of these systems. There are multiple length scales to consider: the critical nucleus size required for the nucleation of ice (<10 nm)^{75,79,80}, the nanoscopic surface roughness (<100 nm)^{57,75,79–81}, the topography needed for superhydrophobicity (50 nm – 10 μ m)^{58,59,62,63,80} and even the macroscopic droplet dimensions⁵⁸. Additionally, one must consider the effect of opportunistic nucleation sites on a sample⁷⁸, droplet impurities^{58,82,83}, surface chemistry^{78,79,82,83}, and environmental conditions such as wind, temperature and humidity^{75,77,78,84}. All of these factors can work in concert or competition, leading to results that are often difficult to decipher.

Classical nucleation theory has been well-studied with regard to a number of phase change scenarios⁸⁵, and is commonly applied to icephobic surfaces. Those who have reported nucleation delay on SHS generally attribute this property to the insulating effect of the air pockets situated between the topographical features of SHS, reduced solid–liquid contact area, and an increased free-energy barrier to heterogeneous nucleation on SHS^{57–59,62,63,80}. Freezing delays were observed to be two orders of magnitude longer on microstructured SHS compared with hydrophilic surfaces at surface temperatures of -20°C ; however, ice formed within seconds once the surface temperature was reduced to -25°C ⁶². At low supercooling temperatures, it was suggested that homogeneous nucleation in the droplet and at the air/water interface dominate ice formation, limiting the effectiveness of surface-based approaches that prevent heterogeneous nucleation⁶². SHS designed using 20-nm particles were found to have a lower ice nucleation probability than those designed with particles larger than 100 nm, possibly because of the higher free-energy barrier for nucleation on the convex surface of 20-nm particles compared with those with greater radii of curvature⁵⁷; however, the results can also be explained by the superior pressure stability of nanostructured surfaces.

Analysing surfaces with a range of chemistries and topographies, Jung *et al.* found that hydrophilic surfaces with minimal roughness (1.4–6 nm) had the longest freezing delay time, followed by hydrophobic surfaces with similar roughness, microstructured SHS, and finally hydrophilic microstructured surfaces⁷⁹. The lower rate of ice nucleation on nanometre-smooth hydrophilic surfaces compared with equivalently smooth hydrophobic surfaces was also reported in experiments that eliminated the effect of droplet impurities by incorporating controlled evaporation, condensation, and freezing processes^{82,83}. While Eberle *et al.* found that hydrophilic and hydrophobic surfaces with ultrafine roughness exhibited similar nucleation temperatures (T_N), hydrophilic surfaces at temperatures slightly above T_N had a longer nucleation delay⁸⁰. The presence of a quasi-liquid layer with reduced entropy at the solid/water or solid/ice interface was seen as a key factor for reducing ice nucleation^{79,80,82,83}. By adapting the classical theory of heterogeneous nucleation to account for a quasi-liquid layer, it was suggested that T_N could be lowered by minimising the roughness length scale below 10 nm^{79–81}. This hypothesis is supported by theoretical work proposing that

the hydrogen bond network of water molecules is destabilised between hydrophobic surfaces when the intersurface separation is on the order of 100 nm or less⁸⁶. Eberle *et al.* further demonstrated that hierarchical SHS that combine controlled nanoscale roughness with designed microtextures can increase freezing delays at temperatures slightly above T_N by two orders of magnitude compared with hydrophobic nanostructured surfaces without microtextures⁸⁰. At $-21\text{ }^{\circ}\text{C}$, their hierarchical surface delayed the freezing of a sessile drop by 25 hours⁸⁰.

In nature, organisms such as fish, insects, and plants have evolved to produce antifreezing proteins which suppress ice nucleation and growth in internal fluids, but these proteins are generally not used to prevent external ice accumulation^{87–89}. There have been a number of recent attempts to incorporate these proteins into solid surfaces in order to develop icephobicity^{90–92}. While significant delays in ice nucleation have been displayed using antifreeze proteins that were conjugated with polymer coatings⁹² and directly immobilized on aluminium⁹⁰, one system incorporating antifreeze proteins on aluminium actually showed increased ice nucleation due to favourable interaction of the surface proteins with nucleating ice crystals⁹¹. More research is needed to determine the mechanism of ice nucleation in the presence of surface-bound antifreeze proteins and develop practical strategies involving biomolecules for improved efficacy.

Although these controlled studies into ice nucleation are of great scientific interest, the ability to reduce the nucleation rate in practical scenarios is limited by environmental considerations. At temperatures below the dew point, many of the previously observed relationships governing ice nucleation behaviour on various surfaces could not be replicated^{75,78}. The nucleation of ice on SHS was systematically studied in an environmentally controlled wind tunnel, with tunable humidity and wind speed⁸⁴. Under static conditions, the previously reported nucleation delay was observed; however, as shown in Fig. 2c, when there was a moderate flow of unsaturated gas, evaporative cooling of the water at the liquid/vapour interface induced homogeneous nucleation before heterogeneous nucleation at the solid surface⁸⁴. A further consideration is surface contaminants, such as dust or salts, which serve as nucleation sites and lead to ice propagation across the surface^{78,93}. These issues highlight some of the challenges facing icephobic materials in real-world environments. Even when heterogeneous nucleation is avoided on the surface itself, it is still possible for ice to accumulate.

Outlook. Although the majority of work in this area has focused on the use of SHS owing to their unparalleled ability to shed liquid water through bouncing, limitations, particularly regarding humidity tolerance, have led some to explore alternatives. Sun *et al.* were able to improve the performance of SHS by combining an inner hydrophilic membrane suffused with a freezing-point depressant with an outer porous SHS, which separated the membrane from the environment⁷⁶. Under dry conditions, the surface behaved like an ordinary SHS but when water penetrated the structures (under high pressure or humidity),

the freezing-point depressant mixed with the water and prevented ice accumulation on the surface⁷⁶. Techniques like this may be necessary to provide icephobic surfaces that are robust enough to survive a wide range of conditions, although the need for freezing-point depressants may preclude some applications. Another option is to employ surfaces with stable lubricant interfaces^{26,30}. Whereas droplet motion on SLIPS is typically slower than on SHS due to viscous dissipation in the lubricant⁹⁴, the stability of the lubricant film under high droplet impact pressures^{26,95} and their high humidity tolerance²⁶ may make SLIPS a viable alternative to SHS in some scenarios. The lubricated systems have predominantly been studied in frosting environments or in the context of ice adhesion, as we will discuss further in later sections.

Frost Formation from Atmospheric Humidity

Although freezing experiments of impinging droplets are often carried out in low-humidity environments to eliminate the effects of condensation, performance in high-humidity environments is critical to many applications. For example, thermal management systems require that the condensate is promptly removed from the surface as it accumulates; otherwise, owing to thermal conductance, water and frost will inhibit heat transfer^{42,52}. Lubricant-infused surfaces, along with some specially-designed superhydrophobic surfaces, have shown promise in the rapid removal of condensation, thereby delaying frost formation under humid conditions.

Limitations of Conventional Superhydrophobic Surfaces. When the temperature of a solid material falls below the dew point, water condensation ensues on the surface. On SHS, condensed water droplets have been shown to nucleate and grow indiscriminately within hydrophobic microscale structures (Fig. 3a), as predicted by classical nucleation theory, which dictates that surfaces with spatially-uniform interfacial energies will exhibit homogeneous nucleation energy barriers^{81,96–100}. The larger surface area and confinement due to the microstructures serve to increase the rate of condensation on SHS, which can result in growing water droplets becoming trapped in the immobile Wenzel state^{96–100}. Similar behaviour has been observed for the spatially-nonpreferential desublimation of frost on superhydrophobic microstructures¹⁰¹.

((Figure 3))

This vulnerability toward condensation can adversely affect the designed function of nonwetting surfaces, even in nature^{102,103}. In one case, a water droplet placed onto a surface patterned with fluorinated triangular microspikes was observed to be in the Cassie regime ($CA = 164^\circ \pm 3^\circ$; $CAH = 5^\circ$)¹⁰⁴. However, when the same surface was subjected to oversaturated vapour, water penetrated the cavities after progressive nucleation and coalescence events, resulting in a Wenzel wetting state. Although a relatively large CA of $141^\circ \pm 3^\circ$ was maintained, the contact angle hysteresis (100° – 105°) and droplet adhesion was

significantly increased, thus preventing condensed droplets from being completely removed by external forces¹⁰⁴.

Surfaces incorporating dense nanoscale topography offer promising resistance to condensation-induced wetting and even display antifrosting behaviour^{105–108}. Likely owing to the same mechanisms responsible for the delayed ice nucleation of sessile droplets on hydrophobic nanostructures^{79,80}, condensing droplets on nanostructured SHS also experience longer freezing times^{105–108}. These findings suggest that surfaces with minimized feature sizes that promote a Cassie state with low hysteresis would be more appropriate candidates for applications where liquid droplet mobility is desired during condensation.

Jumping Droplet Phenomenon. During conventional dropwise condensation on a flat hydrophobic surface, condensed water droplets typically exhibit high CAH, leading to large pinned droplets with diameters on the order of the capillary length of water (approximately 2.7 mm), which are only then able to be removed from the surface with the aid of gravity¹⁰⁹. To remove smaller condensed microdroplets from the surface before freezing, new strategies have been developed. One such technique relies on nanostructured or hierarchical SHS which, in certain scenarios, can promote spontaneous ‘jumping-out-of-plane’ removal of water microdroplets powered by the surface energy released upon coalescence (see Fig. 3b)^{110,111}. The spontaneous motion of droplets in such events is affected by various parameters, including the initial droplet volumes, viscous dissipation, surface feature sizes, structural hierarchy and work of adhesion^{101,112–116}.

This phenomenon of rapid removal of merged droplets is responsible for the observed extremely small average droplet size, approximately ranging from 6–30 μm ^{111,114}. However, under conditions of high supersaturation, the emergent droplets transition from mobile jumping droplets to highly-pinned Wenzel droplets, which completely flood the nanostructured cavities. This exposes the inherent limitations of this approach for high-heat-flux applications¹¹⁷. Under high supersaturation conditions, the droplet nucleation density can increase to the point where interactions between adjacent droplets occur on a similar length scale to the nanostructure spacing, causing the eventual formation of pinned liquid films¹¹⁷.

The principle of self-propelled jumping drops has been further applied to subcooling conditions under which droplets are able to repeatedly jump off the surface before heterogeneous ice nucleation can occur¹¹⁸. To circumvent limitations in supersaturation conditions, superhydrophobic nanostructured micropore arrays, with pitch spacing comparable to the diameter of coalescing microdroplets, have been introduced to maximise the liquid/air interfacial area beneath the coalescing microdroplets¹¹⁹. Although frost still forms, originating from physical or chemical defect sites, and eventually spreads over the entire surface via an interdrop frost wave, the growth of this frost front has been shown to be up to an order of magnitude slower on hierarchical SHS compared with a control hydrophobic surface¹²⁰. Spatial control of heterogeneous droplet nucleation sites at the convex edges limits ice bridging and enhances the jumping-

drop effect, which dynamically minimises the average drop size and overall surface coverage of the condensate¹²⁰. Moreover, these nanostructured SHS have also shown promise in active defrosting situations because the growth of frost can occur in a suspended Cassie state, enabling their dynamic removal upon partial melting at low tilt angles and preservation of the underlying surface¹²¹.

Lubricant-Infused Surfaces. In the absence of air pockets, lubricant-infused surfaces can be expected to maintain high performance despite condensation. Under frosting conditions, a hierarchical SHS coating had over 90% of its surface covered in frost in 80 minutes, whereas its SLIPS counterpart experienced less than 20% coverage, mostly originating from edge defects and interdrop wave propagation^{30,120}, as shown in Fig. 4a. This delay can be attributed in part to the high mobility of droplets arising from low CAH, which allowed water droplets less than 600 μm in diameter to depart the surface under gravity before ice nucleation could occur³⁰. An additional factor is the significantly increased supercooling ability (at least 3–4 °C freezing point depression compared with a SHS) of lubricant-infused surfaces. This property possibly arises from a reduction in the number of potential nucleation sites, which was shown to be effective over 150 consecutive freeze–thaw cycles¹²².

The repellency of these coatings can be compromised by a loss of the lubricant overlayer, which can be driven by high shear, evaporation at elevated temperatures, gravity, or as a result of lubricant spreading onto other solid or liquid surfaces^{94,123–126}. As with SHS, detailed investigations have shown the importance of underlying surface roughness on performance. In the case of lubricant-infused structures, nanostructures are critically important for lubricant retention due to the increased Laplace pressure, whereas the larger features of hierarchical structures more readily become exposed at the interface, leading to increased pinning^{31,34,94,124,127}. Lubricant can spread over condensed droplets, as shown in Fig. 4b¹²⁸, which results in subsequent loss of the lubricant overlayer when droplets are shed. Careful selection of lubricant and favourable surface chemistry can prevent this effect and yield enhanced dropwise condensation behaviour³¹. Direct imaging of the microscale dynamics during condensation and frost formation on liquid-infused surfaces has provided insight into the interactions between the four phases (solid substrate, lubricant, water, air)¹²⁹.

((Figure 4))

Rykaczewski *et al.* conducted a detailed study of frost formation on lubricant-infused structured surfaces using cryogenic scanning electron microscopy¹²⁸. This highlighted the importance of nanoscale surface texture and optimised interfacial energies when designing lubricant-infused surfaces. Specifically, on surfaces with underlying microtexture, it was observed that the oil not only drained from the vicinity of a frozen drop, but also from underneath it, where it was permanently displaced by water, suggesting limitations in prolonged droplet shedding operation¹²⁸. In contrast, increased capillary forces produced by

nanotextured surfaces are much more effective in retaining oil within the structures and limiting the subsequent penetration by water³¹. Although the anti-icing performance of these materials has been shown to rival that of state-of-the-art SHS, careful design of the materials system is required to minimise lubricant migration and carry-over to achieve practical longevity.

Outlook. Although superhydrophobicity alone is not sufficient to provide robust anti-frosting surfaces, when these surfaces are further engineered to induce jumping droplets, frost formation can be significantly delayed; however, the delicate nanoscale roughness required to promote jumping droplet behaviour will likely result in surfaces prone to mechanical damage¹³⁰. Alternatively, SLIPS can also shed small condensed droplets. These lubricant-infused surfaces are self-healing but require the overall lubricant level to be maintained above the textured solid, which may limit prolonged operation. The precise nature of condensation on SLIPS is still under investigation and, in some cases, is predicted to occur at the solid/liquid interface¹³¹. Further understanding of this mechanism could influence the design of future frost-repellent materials.

Offering a potentially more robust approach to lubricated nanotextured surfaces, the incorporation of an immiscible oil into a bulk polymer/gel has recently been demonstrated as a high-performance repellent coating^{132–137}. Aside from post-infusion of the polymer matrix with lubricant, it has been shown that the oil can be stored in discrete shell-less microdroplets within the polymer gel to provide a self-regulated liquid secretion directed towards the surface, which can also be made thermoresponsive for anti-icing application^{135,136}. If carefully designed and fabricated, these surfaces can exhibit most of the desirable traits of a functional anti-icing surface, including low surface energy, minimal surface roughness, a mobile oil overlayer and a longevity-enhancing lubricant reservoir. Although this approach offers a solution to lubricant loss by providing a surplus of oil, the underlying mechanism for lubricant depletion and the associated loss rate has not been addressed; for many applications, the additional weight gain and decreased heat transfer may counteract the potential benefits.

Adhesion of Ice Following Freezing

Ice eventually forms on even the best icephobic surfaces under extreme conditions, making the easy removal of ice a critical but challenging requirement for icephobic surfaces. Fundamentally, the strong interaction of ice with most solids can be attributed to Van der Waals forces¹³⁸ and electrostatic interactions¹³⁹, with the latter proposed as the dominant mechanism due to the interaction of electrical charge at the ice surface and induced charge on the solid substrate^{139,140}. Surfaces that incorporate hydroxyl groups can also increase adhesion through hydrogen bonding¹⁴¹. Although covalent chemical bonding

directly associated with the ice surface can be considered, it is limited to very short distances (0.1–0.2 nm) and is only a factor for solids with specific chemical and crystal arrangements¹³⁹.

Although there are many different methods for measuring ice adhesion, the two most common techniques involve freezing a column of ice and shearing it from a surface using a force probe¹⁴², or removing ice with the shear or tensile forces experienced during centrifugation¹⁴³. It is worth noting that absolute values of ice adhesion (*i.e.* the area-normalised force to remove ice) depend on the methods of measurement and ice formation¹⁴⁴. To alleviate discrepancies between results, ice adhesion measurements can be normalised with respect to untreated control substrates, generating adhesion reduction factors but there is no commonly agreed standard surface. Although aluminium is frequently used, variations in the surface quality, for example, due to surface finish or preparation, can still impact the results¹⁴⁴. Thus, it is important to consider the specific methodology used for ice adhesion experiments and for researchers to incorporate adequate control surfaces to facilitate comparison. In Fig. 5, a broad overview is given of ice adhesion values reported in the literature^{30,36,37,60,132,136,137,141,142,145–161}, although this should be used only as a general guide owing to the aforementioned challenges. Ice adhesion below ~20 kPa is seen as the benchmark for surfaces that allow passive ice removal through factors such as wind or vibration; however, an ideal icephobic surface also requires high mechanical stiffness and durability^{155,159,162}. Here we focus on the relationship between water wettability and ice adhesion for smooth and structured surfaces before discussing recent strategies to reduce adhesion using lubricated surfaces.

((Figure 5))

Smooth and Structured Surfaces. Early attempts to minimise ice adhesion employed predominantly smooth surfaces with low surface energy. Polymers such as PDMS¹⁴² and PTFE¹⁶³ have been shown to minimise ice adhesion compared with higher energy substrates, and there are strong correlations between water wettability and ice adhesion^{141,151,158}. A comprehensive study that consisted of a large number of smooth surface coatings identified the practical work of adhesion for water, $W_A = \gamma_{lv}(1 + \cos\theta_r)$, as having the strongest correlation with ice adhesion¹⁵¹, where γ_{lv} is the surface tension of the water/vapour interface and θ_r is the receding contact angle. Because it is impossible to attain a receding contact angle greater than ~120° on smooth surfaces using known chemistries¹⁶⁴, SHS with nano- and microscale roughness were needed to achieve significantly reduced ice adhesion^{61,148–150,165,166}, with typical values in the range of 50–100 kPa¹⁵⁰. These low values of ice adhesion occur when SHS maintain the Cassie state at supercooled temperatures¹⁴⁸ and feature low CAH¹⁵⁰ in addition to high contact angles. The reduced ice adhesion on SHS is explained by the solid/ice interfacial energy, low solid/ice contact area, and the presence of stress concentrators at the tops of microposts that may promote crack initiation¹⁶⁷.

Unfortunately, the durability of these surfaces continues to be a major concern. Repeated icing–shear-removal cycles, and even less rigorous freeze–thaw cycles⁶⁰, have been shown to increase adhesion significantly as high-aspect-ratio surface features tend to be permanently damaged during ice removal^{60,147,152,160}. Furthermore, these surfaces still suffer from poor humidity tolerance, as discussed in previous sections. When water trapped in the Wenzel state freezes, ice adhesion scales with the actual solid/ice contact area, resulting in ice adhesion that is higher than on chemically-equivalent flat surfaces^{101,168}. Others have confirmed that ice formed in humid environments is much more difficult to remove^{152,160}, and may even form within microtextures in unsaturated environments owing to changes in local saturation caused by the latent heat of crystallization¹⁶⁹.

These limitations have renewed interest in the use of smooth surfaces to decrease ice adhesion^{153,155,156}. Silicone-based coatings have been revisited as a potential material for decreasing ice adhesion, achieving very low values^{142,155,156}, but testing viscoelastic polymer films adds a layer of complexity. Increased film thickness and shear rate during measurement have been shown to increase the ice adhesion on PDMS surfaces, compared with relatively constant values for stiff samples^{155,156}. Furthermore, the low mechanical stiffness and durability of PDMS may make it unsuitable for some applications. Smooth fluorinated surfaces that are stiffer and more durable have been developed in recent years^{153,155}. In particular, smooth sol–gel coatings incorporating perfluorinated polyethers have been used to show an adhesion reduction factor of nearly 20 (approximate ice adhesion of 75 kPa)¹⁵⁵. Maintaining low roughness was seen to be critical to the coating’s performance¹⁵⁵, which was far superior to that of rough fluoropolymers¹⁷⁰.

Surfaces Incorporating Lubricant. Surfaces that incorporate a lubricating liquid have the potential to significantly reduce ice adhesion. Ice adhesion of ~15 kPa was achieved on SLIPS³⁰ and very low ice adhesion (~10–100 kPa) was observed on structured lubricant-infused surfaces^{36,37,154,157}. These surfaces are thus at the upper threshold (*i.e.* ~20 kPa) for self-removal of accreted ice by vibration or wind^{155,159,162}. Subramanyam *et al.* studied the dependence of ice adhesion on the lubricant level and found that the ice adhesion increased significantly as excess lubricant above the posts was depleted; however, the extent to which ice adhesion increased was mitigated by spacing posts closely together¹⁵⁴. Although it may seem counter-intuitive that the surface with the highest solid fraction performed the best, the authors argued that ice adhesion was minimised by the high density of crack initiation sites at the edges of the posts¹⁵⁴. Another effect that may contribute to decreased ice adhesion is the superior lubricant retention of closely spaced posts due to the increased Laplace pressure¹²⁷, which would allow closely spaced posts to maintain a smoother substrate/ice interface. Both factors should contribute to further reduced ice adhesion for lubricated surfaces incorporating nanostructures. As discussed with regard to frost formation, the longevity

and durability of the lubricant-infused surfaces are significant challenges for their implementation as icephobic surfaces, and the strategies discussed for improvement in that context remain critical.

Very low ice adhesion has been demonstrated using lubricant-infused polymer systems^{132,136,137,142}, and infused polymers can be expected to maintain low ice adhesion even once the lubricant is depleted owing to their generally low surface energy and smooth surfaces. The ice adhesion of PDMS has been shown to decrease when silicone oil is mixed with the uncured PDMS precursors^{132,142}. Similar effects can be achieved by swelling the cured polymer network with compatible oils^{134,137}. Using liquid-paraffin as the infused oil in a PDMS network, Wang *et al.* were able to achieve extraordinarily low ice adhesion of only 1.7 kPa at temperatures as low as -70°C , and ice adhesion remained below 10 kPa after 35 icing–removal cycles measured over the course of 100 days¹³⁷. In this case, measurements were spaced over the 100-day period, masking the kinetic aspects of lubricant depletion and replenishment that still need to be studied and understood to characterise the performance of such systems in practical scenarios. Showcasing the importance of understanding lubricant dynamics, almost negligible ice adhesion could be obtained on a surface designed to release lubricant at low temperatures¹³⁶.

One of the more intriguing properties of ice is the presence of a thin liquid-like transition layer at the ice surface, which can make ice slippery and has been used to explain various phenomena, such as the ability of skates to slide easily on ice^{171–175}. Although the existence of pressure- or friction-induced liquid films at the surface are popular explanations for low friction on ice, both theories are largely inadequate and have fallen out of favour compared with arguments that credit interfacial disordering and entropic effects for the presence of a quasi-liquid layer at the ice surface^{171–175}. This effect has been used to reduce ice adhesion on hydrated surfaces that promote the existence of an aqueous lubricant layer without the need for additional oils that become depleted over time^{145,146,159,161}. Although hydrophilic surfaces generally possess high ice adhesion, these surfaces, which are comprised of hygroscopic polymer films^{145,159,161} or polyelectrolyte brushes¹⁴⁶ that swell with water, are capable of suppressing ice nucleation through molecular confinement. There generally exists a transition temperature, ranging from -10 to -53°C , below which the lubricating film is not present and ice adhesion increases drastically^{145,146,159,161}. The transition point can be lowered by tuning the chemistry of the hygroscopic polymer^{145,159,161} and maximising the entropic effect of the counter-ion on the aqueous film¹⁴⁶. The highest performing surface was able to maintain a low ice adhesion value of ~ 25 kPa at temperatures down to -53°C , even after 30 icing–deicing cycles¹⁵⁹.

Outlook. There are a number of promising options for reducing ice adhesion under active development, and lubricated systems in particular have demonstrated extraordinarily low ice adhesion in various studies; however, their longevity and ability to maintain performance in different environments are important

considerations that require further study, in the cases of both infused polymers and structured surfaces. Another concern for these materials, including those that maintain aqueous lubricant layers, is their ability to withstand mechanical abrasion and damage. By cross-linking a hygroscopic polymer inside silicon micropores to protect the bulk of the polymer from abrasion, Chen *et al.* made a surface that maintained low ice adhesion after 80 abrasion cycles¹⁶¹, but the durability of these polymer coatings on their own has not been reported. SHS have been studied far more extensively than lubricated surfaces, and, to our knowledge, SHS that demonstrate satisfactorily low ice adhesion along with mechanical durability and cycle tolerance have not yet been demonstrated. Further efforts should focus on increasing durability, for example, by incorporating stronger materials or structures designed to maintain superhydrophobicity after sustaining damage^{130,176}. Many natural structured materials show combinations of strength and toughness that have been difficult to replicate synthetically. It is possible that further understanding of the origin of these properties may inspire or inform the development of new, tougher structured surfaces that can yield more durable icephobicity¹⁷⁷. Continued investigation into smooth surfaces may be worthwhile, as their simplicity and durability may make them the most industrially feasible avenue for many applications, particularly when lubrication is not possible.

Perspective

Ice accumulation poses significant challenges in building infrastructure, marine applications, aerospace, refrigeration, power transmission, telecommunications and other industries. In this Review, we have focused on the various ways in which ice forms and passive prevention strategies that have been employed in each scenario. An ideal icephobic surface for many of these applications, however, should perform well in all possible situations. Although progress has been made, no single surface has shown the ability to rapidly shed impacting and condensing water droplets, suppress ice nucleation, and reduce ice adhesion, all while operating in a variety of environments with high durability and longevity. The strategies for developing icephobic materials, as discussed in this Review and shown in Fig. 6, include both dry and lubricated surfaces, spanning a range of chemical functionalities and length scales.

((Figure 6))

Superhydrophobic surfaces excel owing to their ability to shed water but in spite of extensive research, issues of humidity tolerance and durability during ice removal persist. SHS may be most effective when used in controlled environments, such as for heat exchangers, where the jumping droplet effect can delay frost formation and the surface can be maintained with limited exposure to the external environment. The ease of application and simplicity of smooth surfaces may make them attractive for applications in harsher environments. Although the lack of nano- or micro-structuring can make smooth surfaces more robust, roughness developed through erosion may still hinder repellency^{155,170}.

Hydrated surfaces with aqueous lubricating layers offer the advantage of simplicity and longevity because the lubricant can be replenished by atmospheric moisture; however, performance outside of ice adhesion remains unreported. It can be expected that hydrophilicity will lead to poor resistance against impinging droplets and condensation. Further testing in a variety of environmental conditions is needed to demonstrate the viability of these hygroscopic polymers as widely applicable icephobic materials.

Surfaces incorporating hydrophobic lubricating layers continue to show extremely high promise, despite tempered expectations owing to current limitations on longevity. We anticipate that optimisation of topographical length scale, surface functionality, and lubricant chemistry will be able to minimise these concerns. It is important not only to consider the empirical optimisation of these parameters, but also to gain a deeper understanding of the interactions between components of this complex system. The presence of excess oil in the bulk of an infused polymer may improve longevity compared with structured surfaces. Furthermore, a degree of icephobicity should be maintained upon depletion owing to the remaining smooth, low-energy surface of the polymer. Future research should focus on durability, longevity and potential replenishment of these lubricant-infused surfaces rather than achieving maximum performance under ideal conditions.

Although passive icephobic materials continue to be improved, each has limitations in some aspects of icephobicity. By understanding the successes and failures of each technology, it may be possible to design surfaces that incorporate features from multiple strategies to further improve versatility. Ultimately, it may be necessary to use ice-repellent surfaces to augment, rather than completely eliminate, traditional anti-icing and deicing techniques. The work of Sun *et al.*⁷⁶ stands out as a method for reducing the amount of deicing fluid used on airplanes by incorporating a SHS. Such a technique might also be combined with biological or biomimetic antifreeze proteins to offer a more environmentally friendly solution. One can imagine similar strategies, such as surfaces with low wettability being used to decrease the amount of heating needed to remove ice, or lubricant-infused surfaces that release lubricant only during specific loading conditions. The integration of icephobic materials with current technologies has not seen extensive study, but is an important consideration for the eventual application of these technologies.

Acknowledgements

The authors would like to thank Drs. Alison Grinthal and Kyoo-Chul Park for their comments on the manuscript. MJK would like to thank NSERC for a PGS D scholarship. The information, data, or work presented herein was funded in part by the Advanced Research Projects Agency-Energy (ARPA-E), U.S. Department of Energy, under Award Number DE-AR0000326.

Competing Interests Statement

JA and PK are founders of SLIPS Technologies, Inc.

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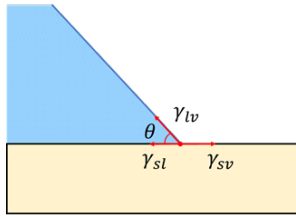
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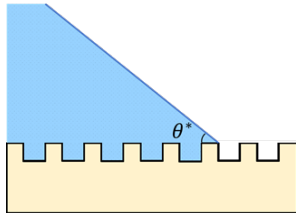
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Young's Equation

$$\cos(\theta) = \frac{\gamma_{sv} - \gamma_{sl}}{\gamma_{lv}}$$

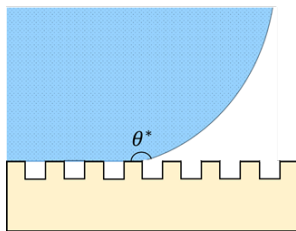
The shape of a liquid drop deposited on an ideal solid (smooth and chemically homogeneous) is dictated by an equilibrium of forces at the contact line formed by the three phases. Young's equation relates the equilibrium contact angle (CA) of the droplet (θ) to the specific energies of the solid-liquid (γ_{sl}), solid-vapor (γ_{sv}), and liquid-vapor (γ_{lv}) interfaces.



Wenzel's Equation

$$\cos(\theta^*) = r \cos(\theta)$$

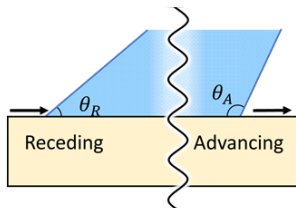
Most surfaces feature some level of roughness, which can cause significant deviation from the ideal surfaces described by Young's equation. If a liquid drop forms a continuously wetting interface along the topography of a solid surface, the apparent CA (θ^*) can be defined by the Wenzel equation, where r is the roughness factor, a ratio of the actual surface area to the projected surface area of the solid.



Cassie-Baxter Equation

$$\cos(\theta^*) = -1 + \phi_s [\cos(\theta) + 1]$$

In the Cassie-Baxter state, liquid droplets do not fully conform to the topography of hydrophobic solids and rest on a composite interface comprised of the peaks of the solid texture and trapped air pockets. This form of the Cassie-Baxter equation incorporates the relative contributions from the substrate and air pockets on the CA of the liquid droplet, where ϕ_s is the solid area fraction of the substrate contacting the liquid droplet. The equation can be generalized to apply to surfaces with heterogeneous surface energy.



Contact Angle Hysteresis

$$\Delta\theta = \theta_A - \theta_R$$

Movement of the contact line can lead to variations in CA owing to surface protrusions, adhesion hysteresis, heterogeneity, and thermodynamic considerations. The largest CA observed before the contact line advances is recognized as the advancing CA (θ_A). Conversely, the smallest CA observed before the contact line recedes represents the receding CA (θ_R). The difference between these contact angles is defined as the contact angle hysteresis (CAH). Surfaces with low CAH allow for high mobility droplets with low adhesion.

Textbox 1: Key concepts in liquid–solid interactions.

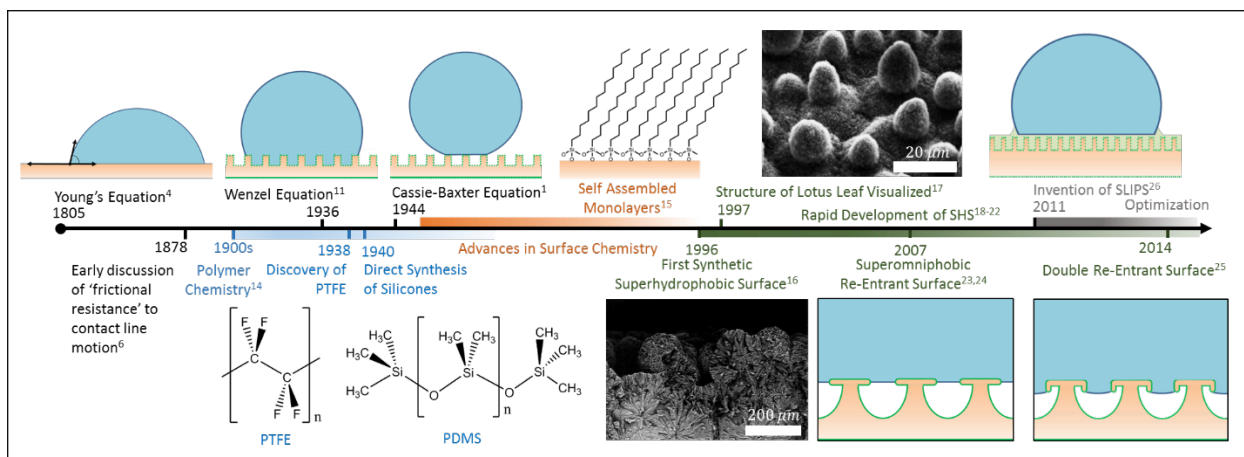


Figure 1: Timeline of major advances in the area of liquid repellency.

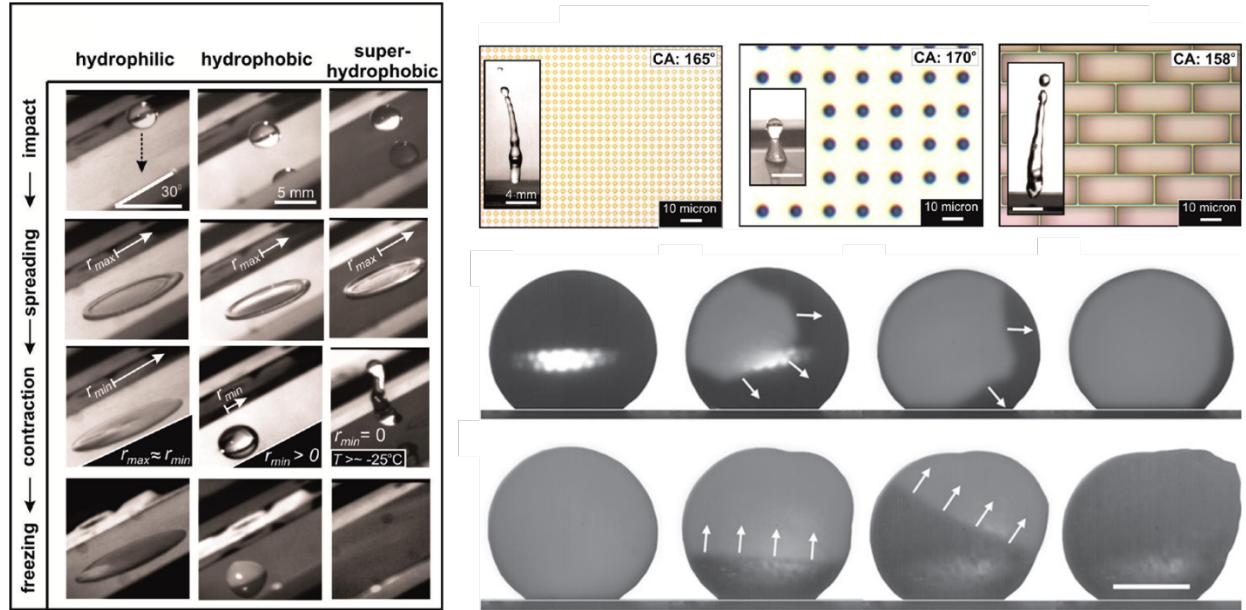


Figure 2: a) Droplets impacting a hydrophilic surface (I), a hydrophobic surface (II) and a SHS (III). Only on the SHS are droplets able to fully retract and shed before freezing⁵⁹. b) Droplets are able to bounce on closely-spaced posts (I) and a closed-cell architecture (III), whereas they pin in the Wenzel state on posts with a larger spacing (II)⁵². c) (I–IV) Partial freezing initiated at the surface of a droplet exposed to unsaturated nitrogen flow (6-ms intervals between snapshots) and (V–VIII) final crystallisation of ice controlled by heat transfer with the substrate ($t = 0, 5, 9$ and 13 s)⁸⁴.

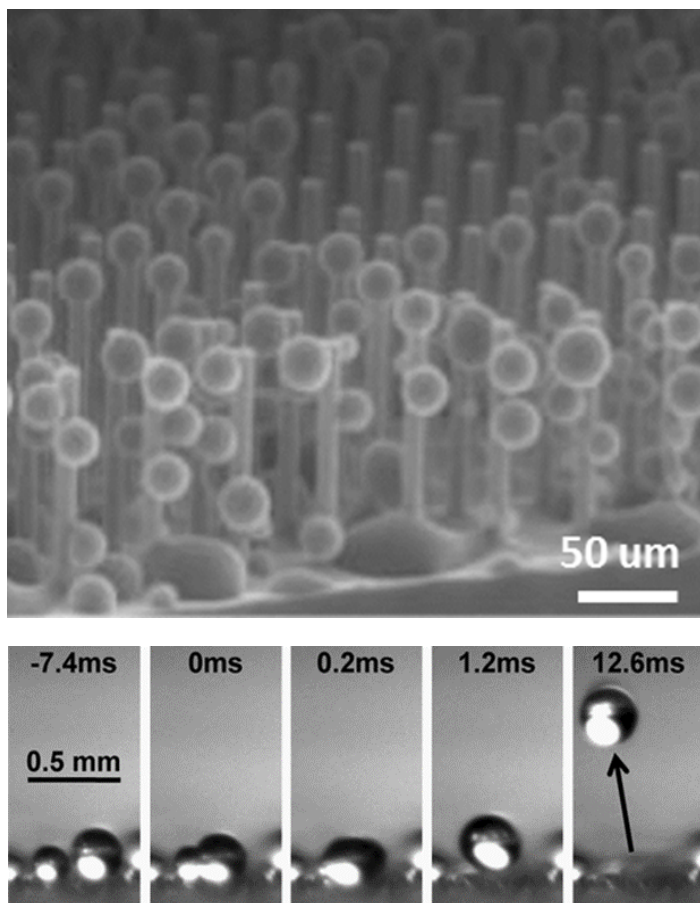


Figure 3: (a) Environmental scanning electron microscopy images of the water vapor condensation behaviour on a microstructured SHS, where owing to the chemical homogeneity of the surface, droplet nucleation occurs without apparent spatial preference. As these droplets grow and coalesce, Wenzel-type droplets are eventually formed¹⁰⁰. (b) High-speed imaging time-lapse of autonomous out-of-plane droplet removal via dynamic coalescence witnessed on a hierarchical SHS with extremely low adhesion forces¹¹¹.

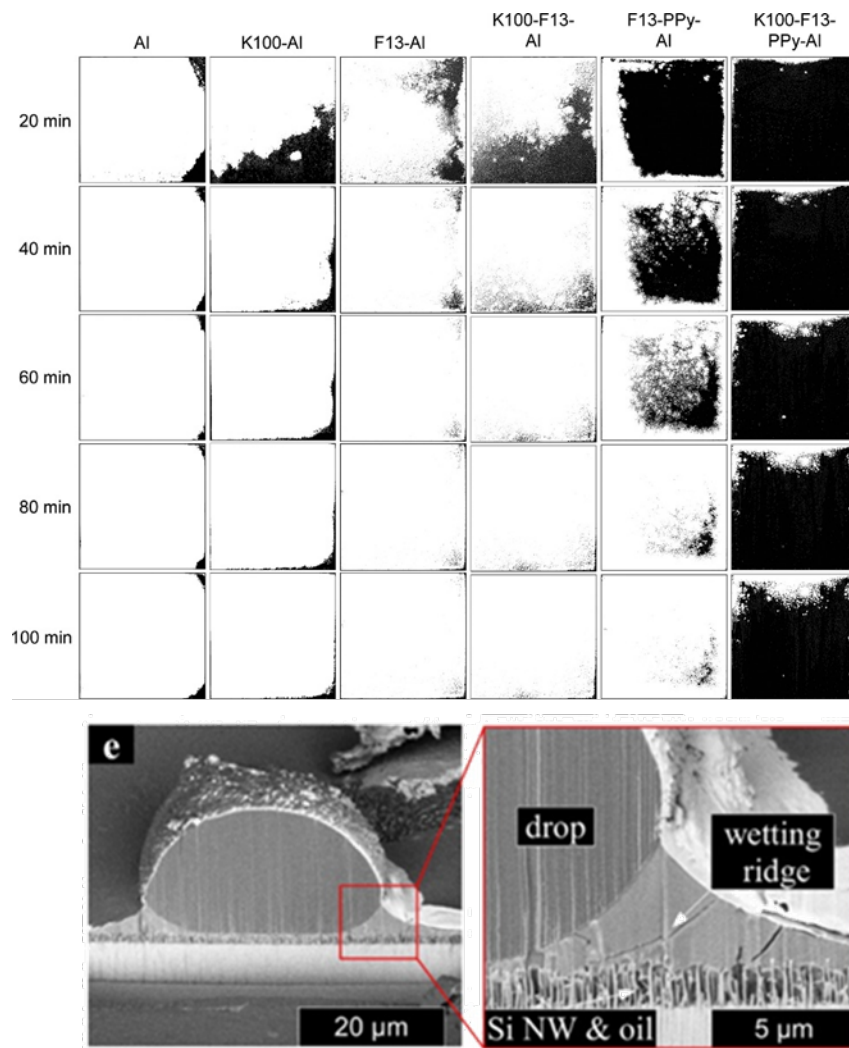


Figure 4: (a) Time-lapse threshold images of frost formation (frost-covered areas shown in white) on various large-scale aluminium surfaces (from left to right: bare aluminium, greased aluminium, hydrophobic aluminium, greased hydrophobic aluminium, hydrophobic hierarchical polypyrrole coating and a lubricant-infused polypyrrole coating). After 100 min of freezing, ~99% of all control surfaces are covered with frost, except for the lubricant-infused polypyrrole coating, on which frost coverage was suppressed to only 20% of the area³⁰. (b) Environmental scanning electron microscopy images of a frozen droplet on a lubricant-infused silicon nanowire surface, demonstrating the spreading and encapsulation of the droplet by the lubricant that can occur in unfavourable system configurations. Samples were cross-sectioned using a cryogenic focused ion beam¹²⁸.

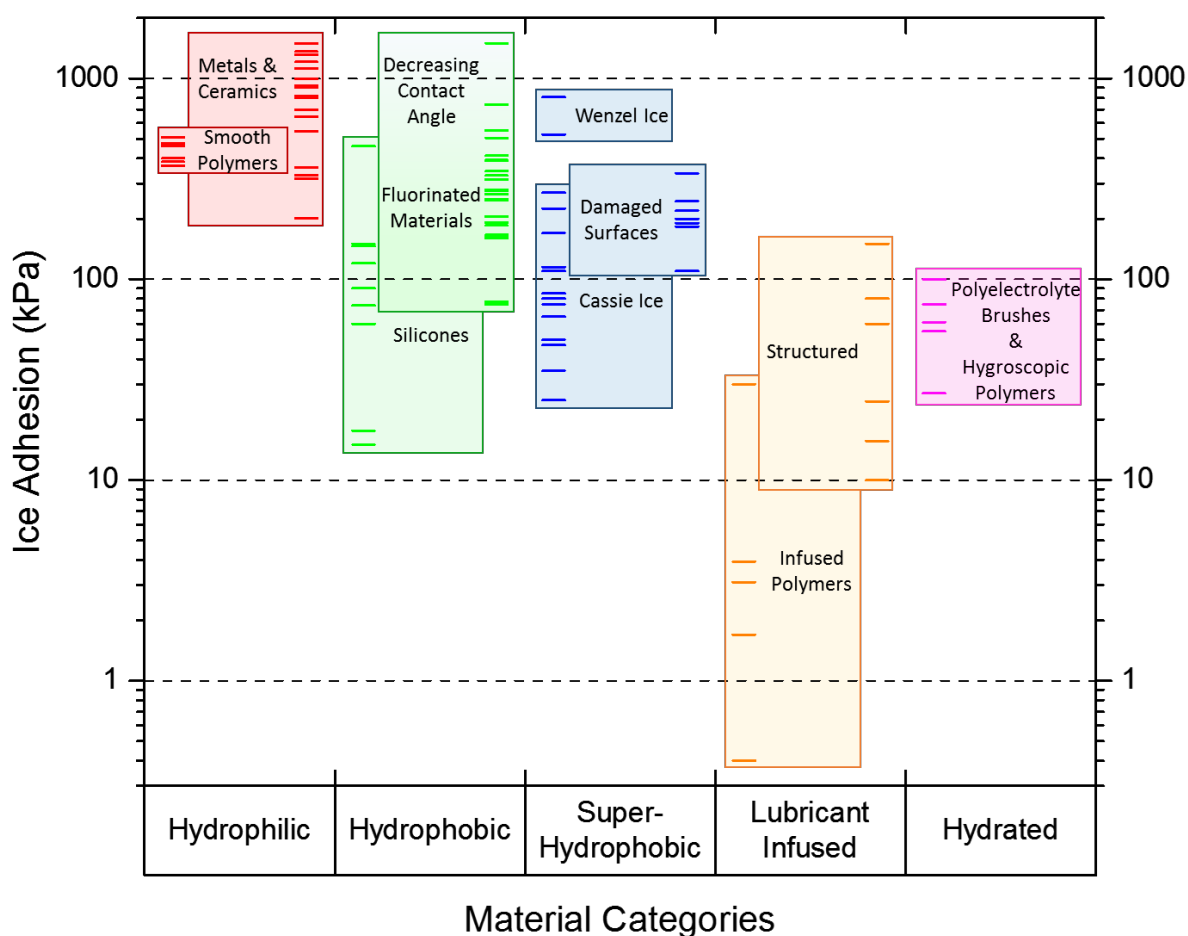


Figure 5: Ice adhesion values reported in the literature for different types of surfaces^{30,36,37,60,132,136,137,141,142,145–161}. Owing to the difficulty in comparing ice adhesion measurements generated using different protocols, values and regions are not statistically defined, and should be considered as general guides.


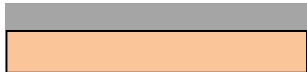
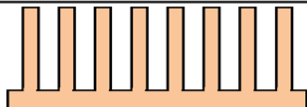
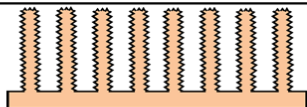
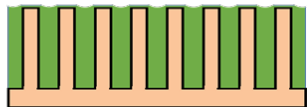

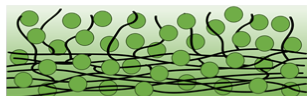

				references
Dry Interface	Smooth	 SAMs	<ul style="list-style-type: none">• Environmentally tolerant• Limited surface compatibility• Lower performance than state-of-the-art	141,142,151,153, 155,156,163,170
		 Polymer	<ul style="list-style-type: none">• Environmentally tolerant• Versatile and durable• Lower performance than state-of-the-art	
	Textured	 Microstructured	<ul style="list-style-type: none">• Rapid shedding of droplets prevents ice nucleation• Poor pressure and humidity tolerance, durability	57–63,72,74–76, 78–80,84,101, 105–108, 118–121, 147–150,152, 158,161,165–170
		 Hierarchical	<ul style="list-style-type: none">• Improved pressure stability• Improved humidity tolerance (jumping droplet effect)• Poor durability	
Wet Interface	Smooth	 Microstructured	<ul style="list-style-type: none">• Low ice adhesion and droplet CAH• High humidity tolerance• Poor resistance to lubricant depletion	30,32,36,122, 128,154,157
		 Nanostructured	<ul style="list-style-type: none">• Improved lubricant retention• Poor mechanical robustness	
		 Infused Polymer	<ul style="list-style-type: none">• Increased lubricant content• Kinetics of lubricant depletion and replenishment unknown	132,136,137,142
		 Hydrated	<ul style="list-style-type: none">• Low ice adhesion without need for lubricant replenishment• Poor wetting properties	145,146,159,160

Figure 6: Comparison of primary strategies for achieving passive icephobicity.